416

國立臺灣大學 106 學年度碩士班招生考試試題

電磁學(C)

題號:416

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	請於 <u>答案卷上非選擇題作答區</u> 標明題號作答。計算題請詳列過程。 $\epsilon_0=10^{-9}/(36\pi)$ [F/m], $\mu_0=4\pi\times10^{-7}$ [H/m]
١.	(填充題) (6%) A transmission line is 30 cm long. It is short-circuited at left end and open-circuited at right end. The lowest two frequencies of its natural oscillation are MHz and MHz.
2.	(填充題) (10%) The directivity of a rectangular aperture antenna is $D=4\pi wh/\lambda^2$ , where w and h are the width and height of the aperture, respectively.
	<ul> <li>(a) (3%) If D of an antenna is 4.0 at 900 MHz, D will be about (1.0, 2.0, 4.0, 8.0, 16.0) at 1800 MHz.</li> <li>(b)(2%) From the equation, you can find that D will be (smaller, the same, larger) for larger w.</li> <li>(c) (2%) From the equation, you can find that D will be (smaller, the same, larger) for smaller h.</li> <li>(d)(3%) The width and height of an edge-emitting laser facet are w = 10 μm and h = 5 μm, respectively. The facet looks like</li></ul>
	(計算題) (12%) Let us consider a uniform plane wave incident from space $(z < 0)$ normally onto an anisotropic perfect dielectric medium $(z > 0)$ , characterized by the permittivity matrix $[\varepsilon] = \varepsilon_0 \begin{bmatrix} 9 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 0 & 4 \end{bmatrix}$ and $\mu = \mu_0$ . The electric field of the incident wave is expressed by $E_i = E_0 \cos(\omega t - k_0 z)(a_x + ja_y)$
	$E_i - E_0 \cos(\omega \epsilon - \kappa_0 \epsilon) (\omega_x + j \omega_y)$

- (a) (8%) Please write the electric-field expressions for the reflected and transmitted waves. (Hint: Consider x-component first, then y-component.)
- (b)(4%) If the wavelength is  $\lambda_0 = 1.5 \mu m$ , please find the shortest distance that the transmitted wave becomes a linearly polarized wave.
- 4. (計算題) (10%) A transmission line of characteristic impedance  $Z_0 = 50 \Omega$  provided the following data. First, the voltage minima were found to be 30 cm apart as it is short-circuited. As the short circuit was replaced by a load  $Z_R$ , the SWR was found to be 4 and a voltage minimum was found to be 6 cm from the reference point on the side toward the load. Please find the  $|\bar{\Gamma}_R|$  and  $\theta$  of the reflection coefficient  $\bar{\Gamma}_R = |\bar{\Gamma}_R|e^{j\theta}$ .
- 5. (計算題) (12%) The  $\omega$ - $\beta$  curve for a dispersive channel can be approximated by  $\beta = \beta_0 + \beta_1 \left(\omega \frac{2\pi c}{\lambda_0}\right) + \frac{\beta_2}{2} \left(\omega \frac{2\pi c}{\lambda_0}\right)^2$  in the vicinity of wavelength  $\lambda_0$ , where c is the light speed in free space.
  - (a) (4%) Please find the phase velocity  $v_{p,A}$  and group velocity  $v_{g,A}$  for signal A at  $\lambda_A = \lambda_0$ .
  - (b)(4%) Please find the group velocity  $v_{g,B}$  for signal B at  $\lambda_B = \lambda_0 + \Delta \lambda$ , where  $\left|\frac{\Delta \lambda}{\lambda_0}\right| \ll 1$ . (Hint: Use  $\frac{1}{1+x} \approx 1-x$  for small x.)
  - (c) (4%) It takes  $t_A$  and  $t_B$  for pulses centered at  $\lambda_A$  and  $\lambda_B$ , respectively, to travel a distance L. If the time difference is  $\Delta t \equiv (t_B t_B)$  $t_A$ ), please find the <u>parameter</u>  $D \equiv \frac{\Delta t}{\Delta T}$
- 6. (計算題) Consider a coaxial cable formed by two perfectly conducting cylinders of radii a = 0.5 mm and b = 2.5 mm with a perfect dielectric ( $\mu_r = 1, \varepsilon_r > 1$ ) filled in between them and the axis of the cylinders is the z-axis. The electromagnetic waves which propagate in the coaxial cable are given by  $\mathbf{E} = \{V_0/[r \ln(b/a)]\}\cos(6\pi \times 10^9 t - 30\pi z)a_r$  [V/m] and  $\mathbf{H} = (I_0/2\pi r)\cos(6\pi \times 10^9 t - 30\pi z)a_\phi$ [A/m] for a < r < b, where  $V_0$  and  $I_0$  are constants.
  - (a) (4%) What is the frequency f of the electromagnetic waves in the coaxial cable?
  - (b)(4%) What is the phase velocity  $v_p$  of the electromagnetic waves in the coaxial cable?
  - (c) (4%) According to (b), what is the relative permittivity  $\varepsilon_r$  of the dielectric filled in between the two conducting cylinders?
  - (d)(4%) Based on (c), what is the capacitance per unit length C of the coaxial cable for static fields?
  - (e) (4%) Based on (d), what is the characteristic impedance  $Z_0$  of the coaxial cable as a transmission line?
  - (f) (4%) Based on (e), if one end of the coaxial cable is open-circuited, what is the voltage reflection coefficient Γ?
  - (g)(4%) Based on (e), if the coaxial cable is terminated with a resistive load without reflection, what is the load reistance  $R_L$ ?
  - (h)(4%) Please find the instantaneous Poynting vector P associated with the electromagnetic waves.
  - (i) (4%) Please find the time-average Poynting vector (P) associated with the electromagnetic waves.
  - (i) (4%) Please find the <u>time-average power flow</u>  $\phi(P) \cdot ds$  along the coaxial cable.
- 7. (計算題) A toroid with magnetic core (permeability  $\mu$ ) of circular cross section (radius = r) as shown in Fig 1. The mean radius of the toroidal core is a and the number of turns per unit length along the mean circumference of the toroid is N.
  - (a) (5%) Please find the magnetic flux  $\psi$  inside the magnetic core when the electric current is I.
  - (b) (5%) Please find the inductance L of the toroid.

